

# Math 10 - Final Exam Formula List

**Policy:** we will explain typos or formatting issues, but not explain the meaning and usage of these equations.

## Summary Statistics

$N$  = population size.  $\mu = \frac{1}{N} \sum_{i=1}^N X_i$ , population mean.  $\sigma^2 = \frac{1}{N} \sum_{i=1}^N (X_i - \mu)^2$ , population variance.

$\sigma = \sqrt{\frac{1}{N} \sum_{i=1}^N (X_i - \mu)^2}$ , population standard deviation.

$n$  = sample size.  $\bar{Y} = \frac{1}{n} \sum_{i=1}^n Y_i$ , sample mean.  $s^2 = \frac{1}{n-1} \sum_{i=1}^n (Y_i - \bar{Y})^2$ , estimate of population variance.

$s = \sqrt{\frac{1}{n-1} \sum_{i=1}^n (Y_i - \bar{Y})^2}$ , estimate of population standard deviation.

## Single Population Standard Errors

Normal:  $\frac{\sigma}{\sqrt{n}}$ . t-distribution:  $\frac{s}{\sqrt{n}}$ , population proportion  $\pi$  known:  $\sqrt{\frac{\pi(1-\pi)}{n}}$ .

If  $\pi$  is not known, and  $p$  = sample proportion then use:  $\sqrt{\frac{p(1-p)}{n}}$ .

## Difference Between Means Standard Errors

Normal:  $\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}$ , t-distribution:  $\sqrt{\frac{2 \cdot MSE}{n}} = \sqrt{\frac{s_1^2 + s_2^2}{n}}$ , where  $MSE = \frac{s_1^2 + s_2^2}{2}$ .

## Regression

Slope coefficient  $b = r \cdot \frac{s_y}{s_x}$ , intercept  $a = \bar{Y} - b\bar{X}$ .  $n$  = number of bivariate data pairs  $(X_i, Y_i)$  in sample.

Degrees of freedom for hypothesis testing is  $n - 2$ .

## ANOVA

$k$  = number of samples/groups,  $n$  = data points in each sample/group.

$N = n \cdot k$  = total number of data points in all groups combined.

$F = \frac{MSB}{MSE}$ . Degrees of freedom:  $df_1 = df_{\text{numerator}} = (k - 1)$ ,  $df_2 = df_{\text{denominator}} = (N - k)$ .

$MSB = \frac{SSQ_{\text{condition}}}{df_{\text{numerator}}} = n \cdot \text{variance of the sample means}$ .

$MSE = \frac{SSQ_{\text{error}}}{df_{\text{denominator}}} = \frac{s_1^2 + s_2^2 + \dots + s_k^2}{k}$ .

## Chi-Square

$\sum \frac{(E-O)^2}{E}$ ,  $E$  = expected frequency,  $O$  = observed frequency.

Degrees of freedom  $df = k - 1$ , where  $k$  = number of categories.